# GNSS-Based Radio Tomographic Studies of the Ionosphere at Different Latitudes

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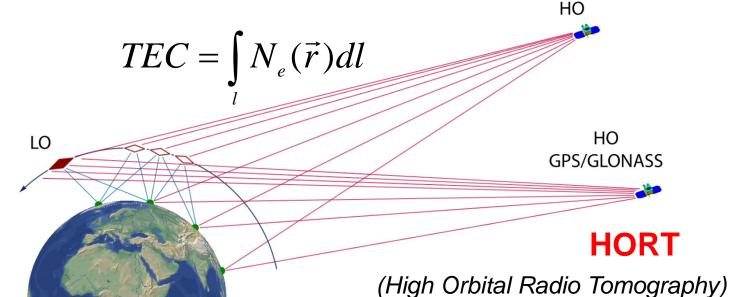
#### **Outline**

- Global Navigation Satellite Systems (GNSS) include:
- new-generation high orbiting (HO) navigation systems (GPS and GLONASS and under development (Galileo, BeiDou, QZSS systems));
- and old-generation low orbiting (LO) navigation systems (Tsikada, Transit, etc.).

The GNSS constellations and the networks of ground receivers are suitable for probing the ionosphere along different rays and processing the obtained data by tomographic inversion procedures. The results are obtained by the methods of low orbiting and high orbiting radio tomography (LORT and HORT, respectively).

- We present the examples of tomographic images of the subequatorial, midlatitude, subauroral, and auroral ionosphere in different regions of the world.
- The GNSS RT methods are suitable for imaging the ionospheric disturbances, waves, TIDs caused by different phenomena including the tsunami wave propagation. We analyze the ionospheric disturbances after the strongest Tohoku earthquake in Japan (March 11, 2011).
- The RT reconstructions are compared to the measurements by the ionosondes and Global Ionospheric Maps (GIM).

## **Methods and Data**



**LORT** 

(Low Orbital Radio Tomography)

"instantaneous" (~5-10 minutes)
2D RT images of the ionosphere
above the receiving chains

{ the horizontal resolution is 20-30 km, and the vertical, 30-40 km. The resolution can be improved up to 20-10 km using dense receiving system and nonlinear RT}

4D RT images (3 spatial coordinates and time)

Typical resolution of HORT is about of **100-50 km** with a time step **60-20 min**.

resolution can be improved up to 30-50 km with a time interval of 30-10 min in the regions with dense receiving networks (West Europe, USA, Alaska) and up to 30-10 km & 2min in regions with very dense networks (Japan, S.California ...)

# Ionospheric Ray Radio Tomography

$$\alpha \lambda r_e \int Nd\sigma = \Phi = \varphi + \varphi_0,$$

$$L$$

- Phase RT PT with estimation of initial phase (RT using linear integrals, including unknows initial phase, определение которых является дополнительной задачей)
- RT using relative phase
- Phase-difference RT RT using difference of linear integrals on close rays (it's not necessary to determine the initial phase)

# Ionospheric Ray Radio Tomograpghy

$$\alpha \lambda r_e \int Nd\sigma = \Phi = \phi + \phi_0$$
, PN =  $\Phi + \xi$ 

LN =  $\Phi + \xi + E$ . E = LN - PN

LN = 
$$\Phi + \xi + E$$
,  $E = LN - PN$   
LN =  $\Phi + \xi$ 

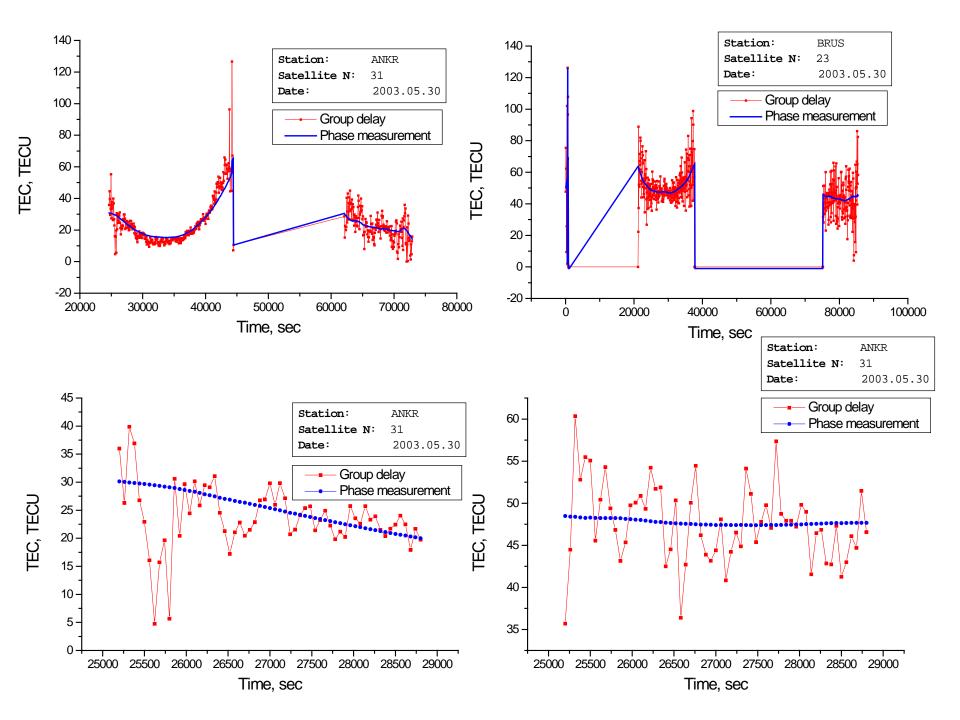
$$- LN = \Phi$$

$$L'N = \Phi'$$

$$AN = \Phi - \Phi' = D$$

20-40км – vertical resolution

10-30км – horizontal resolution



# Solution with Smoothing

$$Af = \Psi$$

$$\min \|f - f_0\|_{W_n^2}^2$$

#### SIRT:

$$\vec{x}^{k+1} = \vec{x}^k + \sum_{i} \rho_i \frac{y_i - (\vec{a}_i, \vec{x}^k)}{(\vec{a}_i, \vec{a}_i)} \vec{a}_i$$

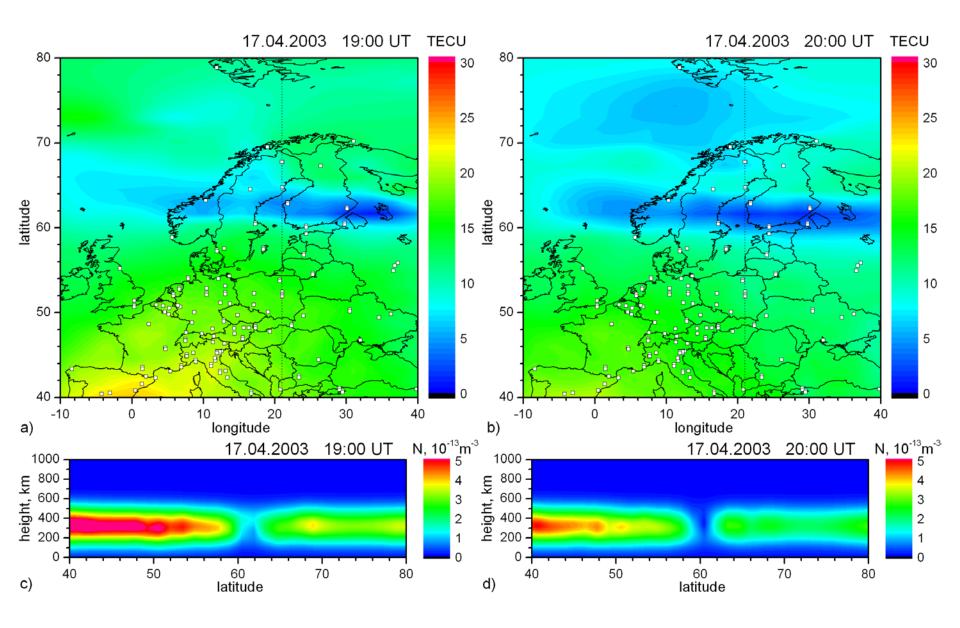
$$\min_{\vec{x} = \vec{y}} \|\vec{x} - \vec{x}_0\|^2$$

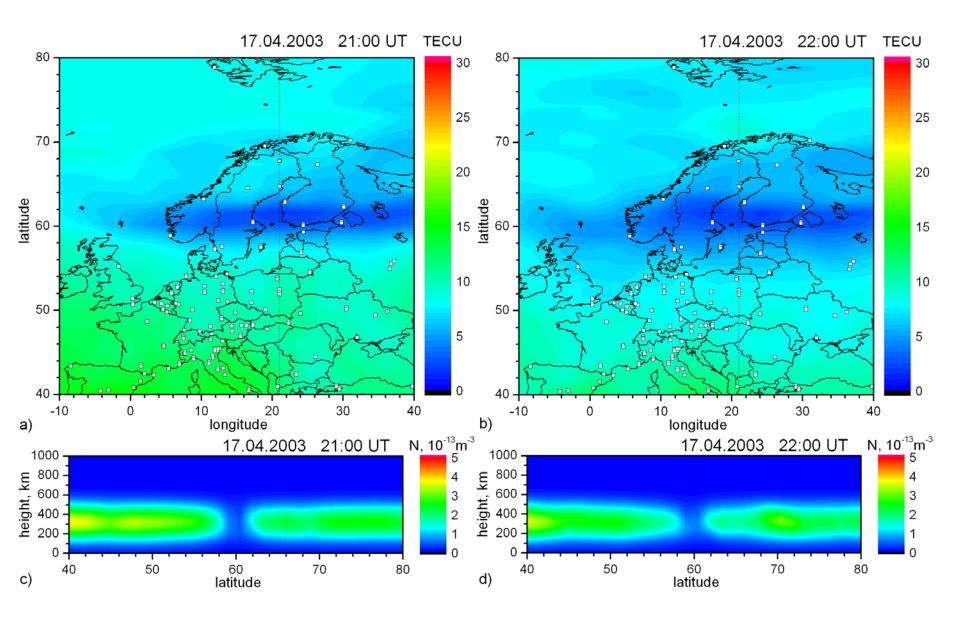
#### **Modified SIRT:**

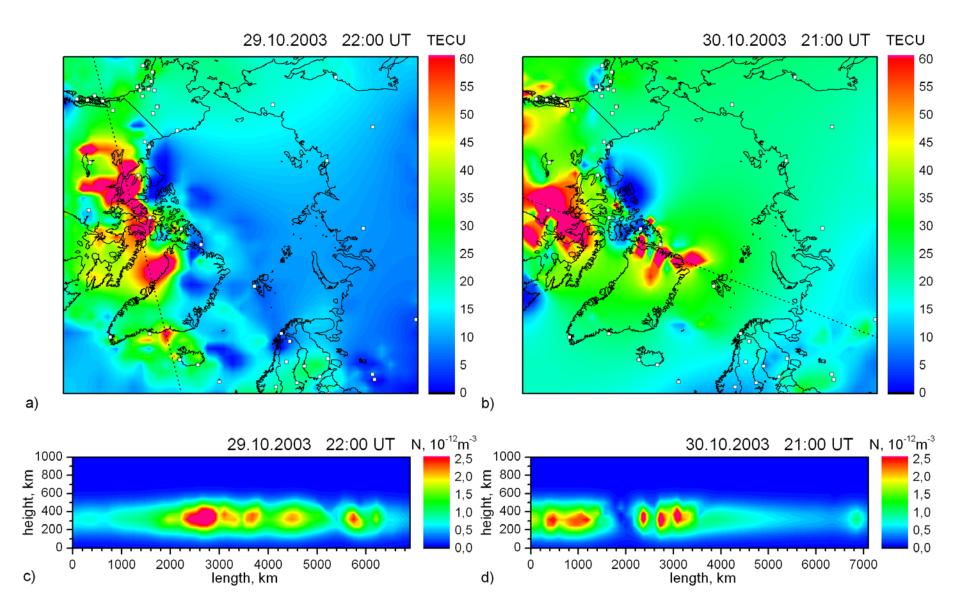
$$\vec{x}^{k+1} = \vec{x}^k + \sum_{i} \rho_i \frac{y_i - (\vec{a}_i', \vec{x}^k)_L}{(\vec{a}_i', \vec{a}_i')_L} \vec{a}_i'$$

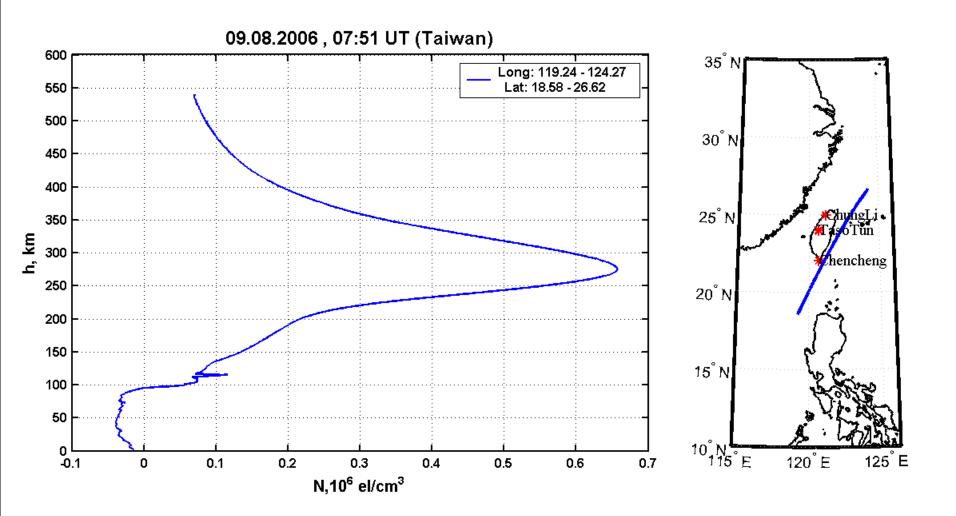
$$\vec{x}^{k+1} = \vec{x}^k + t \left( L^* L \right)^{-1} \sum_{i} \vec{a}_i \left( y_i - \left( \vec{a}_i, \vec{x}^k \right) \right)$$

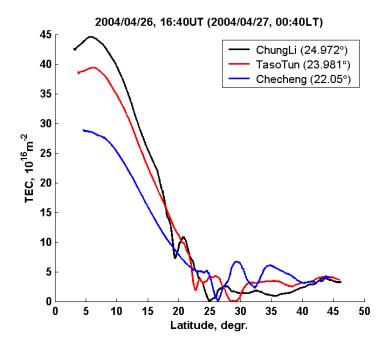
$$\min_{\substack{A\vec{x} = \vec{y} \\ \vec{a}'_i = (L\vec{z}, L\vec{x}) = (\vec{z}, L^*L\vec{x})}} \vec{x} - \vec{x}_0)_L$$



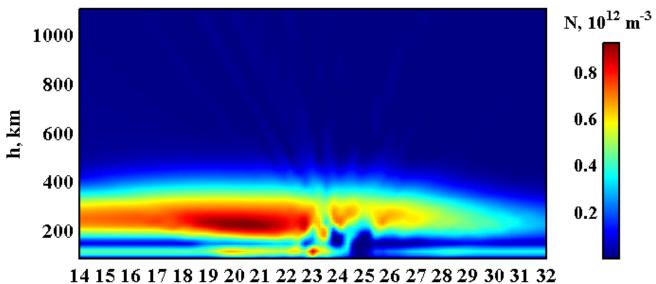




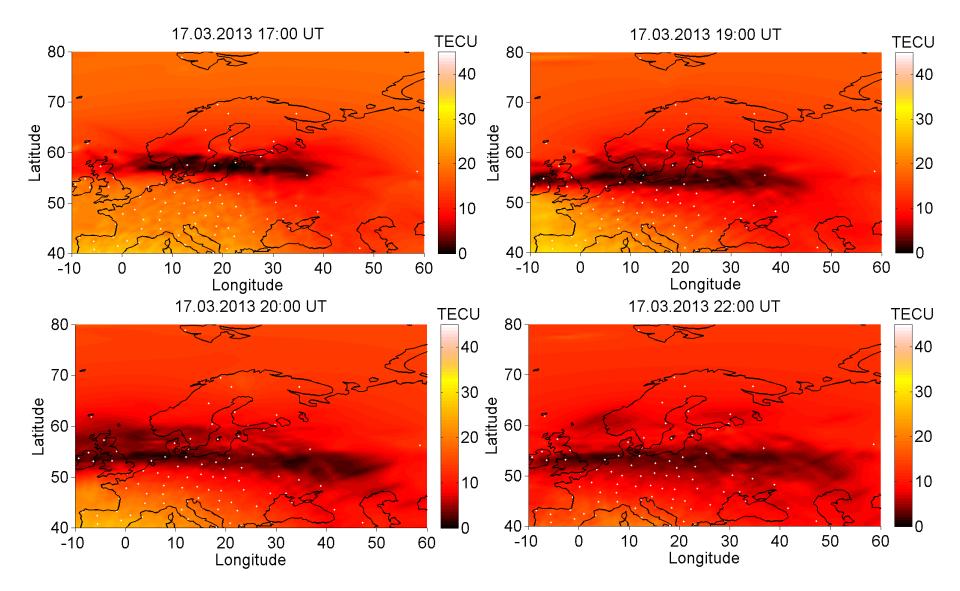




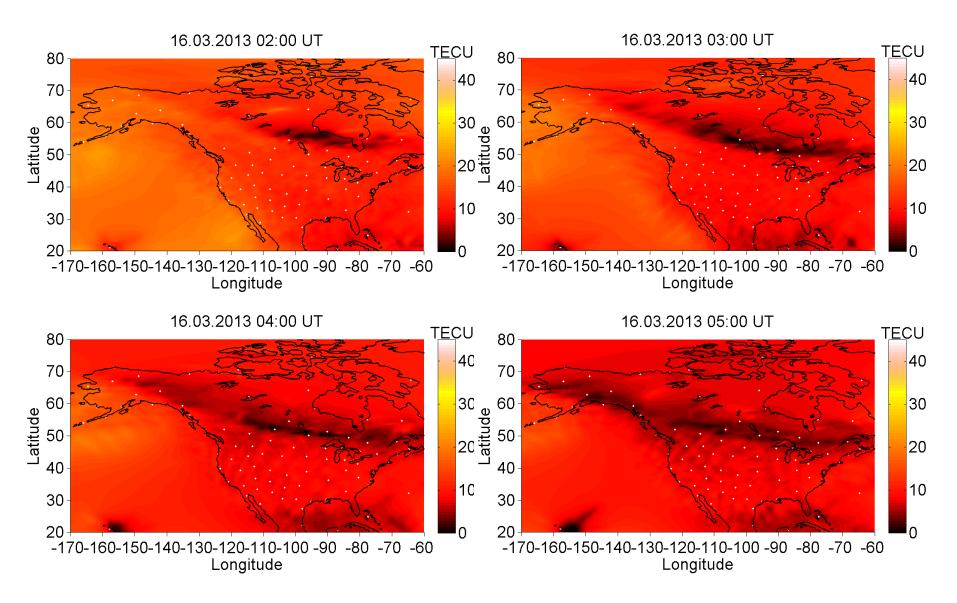
2006/04/26, 16:40UT



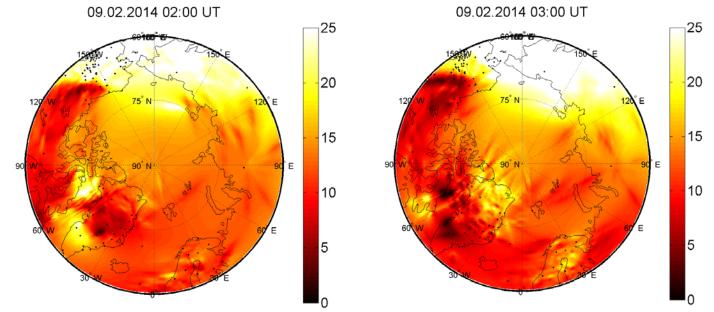
14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 Latitude, degr.



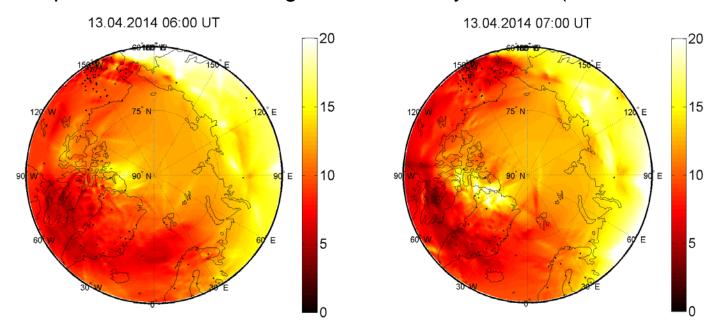
The example of evolution of the ionization trough above Europe on March 17, 2013, 17:00-22:00 UT (Kp=6.7)



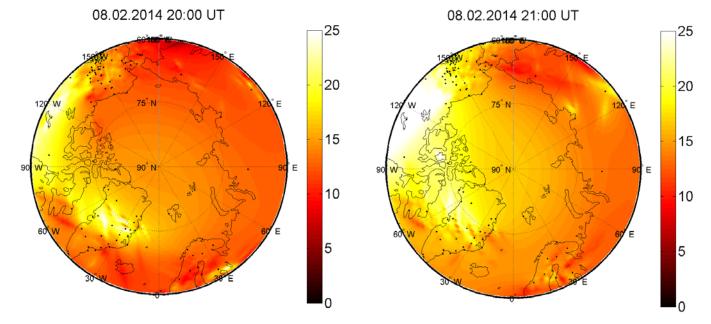
The example of evolution of the ionization trough above North America on March 16, 2013, 02:00-05:00 UT (Kp=3.3)



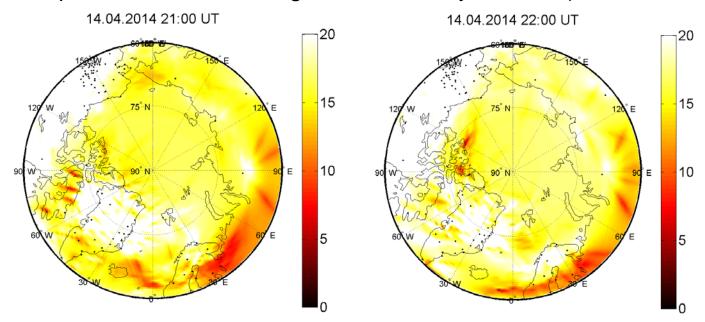
TEC maps above the Arctic region on February 9, 2014 (02:00 and 03:00 UT)



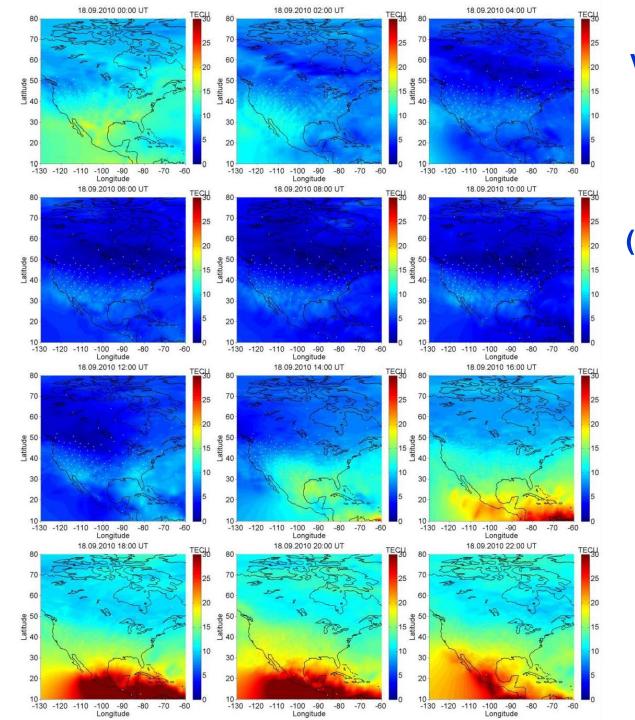
TEC maps above the Arctic region on April 13, 2014 (06:00 and 07:00 UT)



TEC maps above the Arctic region on February 8, 2014 (20:00 and 21:00 UT)

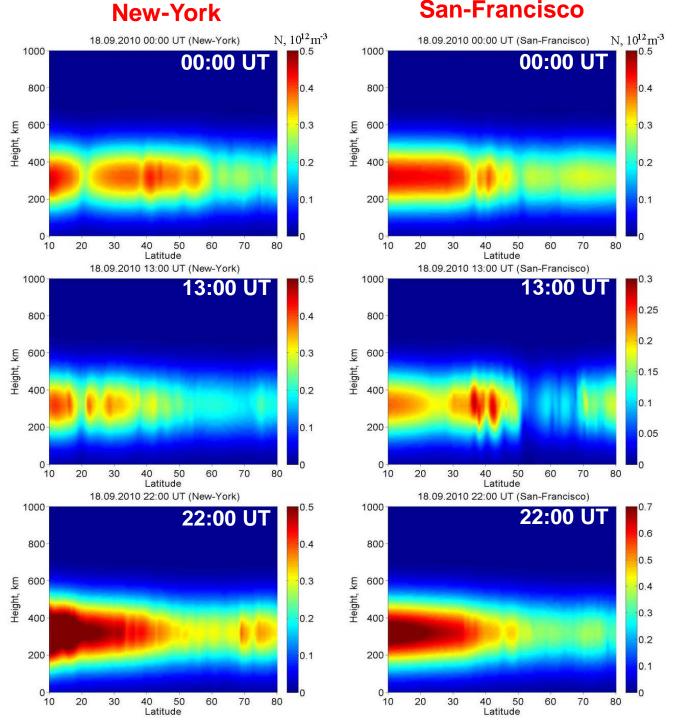


TEC maps above the Arctic region on April 14, 2014 (21:00 and 22:00 UT)

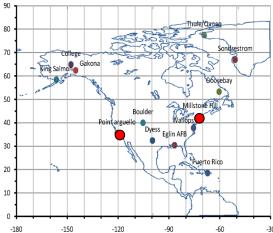


Vertical TEC above
North America
according to
4D HORT during
18.09.2010

(00:00 UT-22:00 UT)

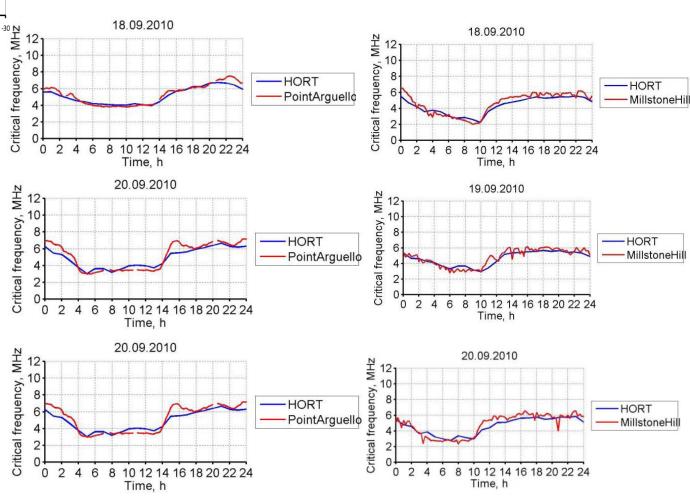


Vertical
cross-sections
of the
ionosphere along
meridians of
New-York and
San-Francisco
according to 4D
HORT during
18.09.2010

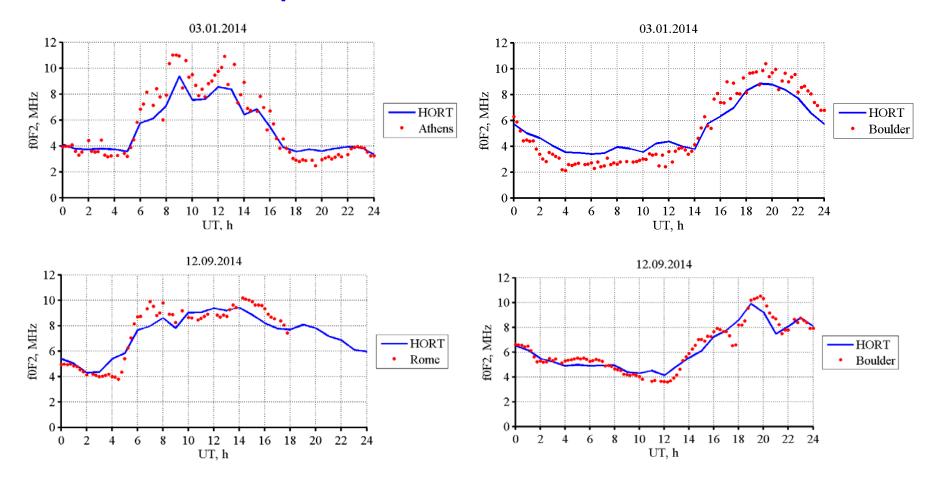


#### Comparison of HORT and ionosonde data

Sept. 18–20, 2010:  $f_oF2$  as obtained from HORTimages and  $f_oF2$  as obtained from Point Arguello ionosonde & Millstone Hill ionosonde.

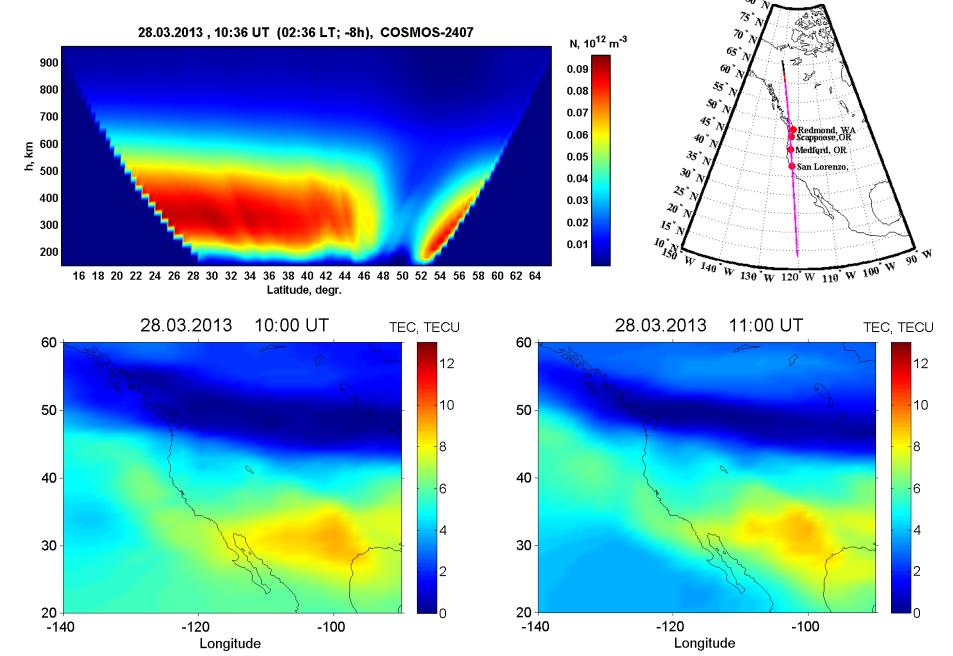


#### Comparison of HORT and ionosonde data

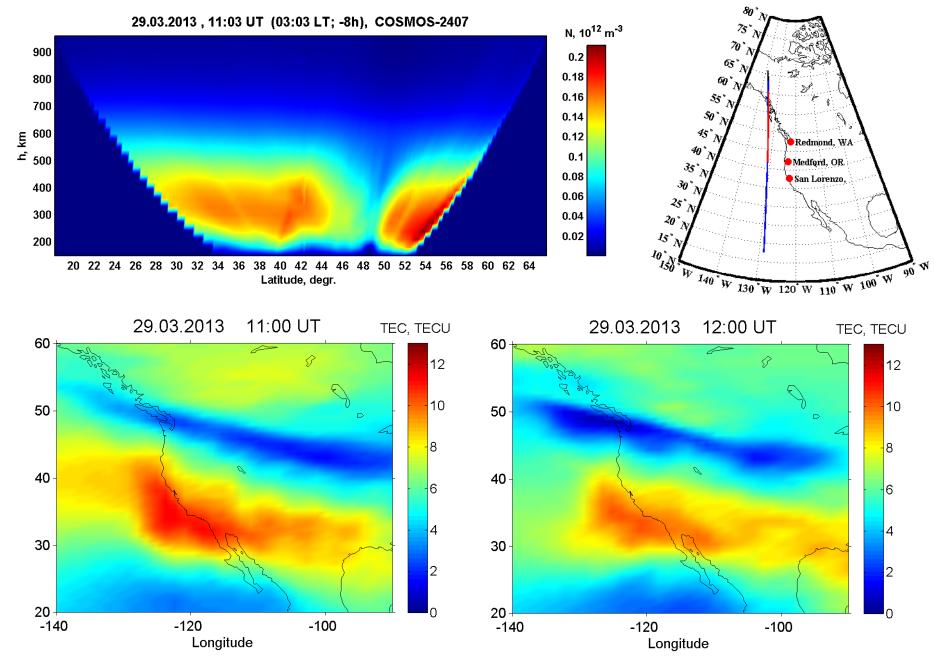


The analysis based on thousands of comparisons indicates that the diurnal behavior of *f0F2* retrieved from HORT quite closely agrees with the ionosonde data. The discrepancies in critical frequencies are far below **0.5 MHz** during the geomagnetically quiet periods and above **1 MHz** during the disturbances.

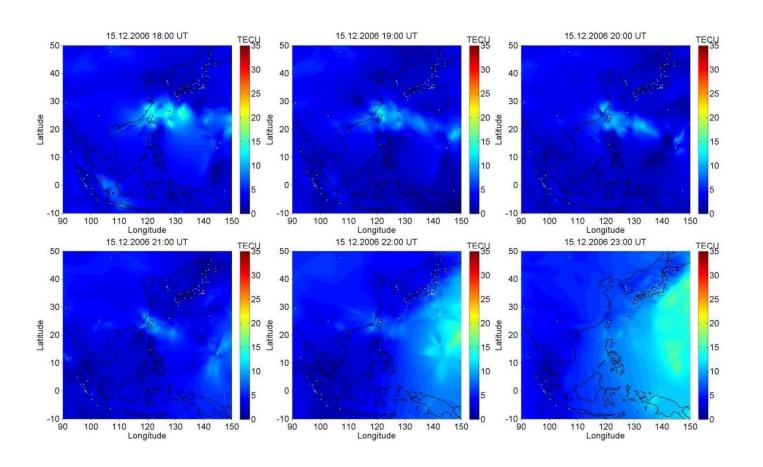
### **U.S. West Coast**

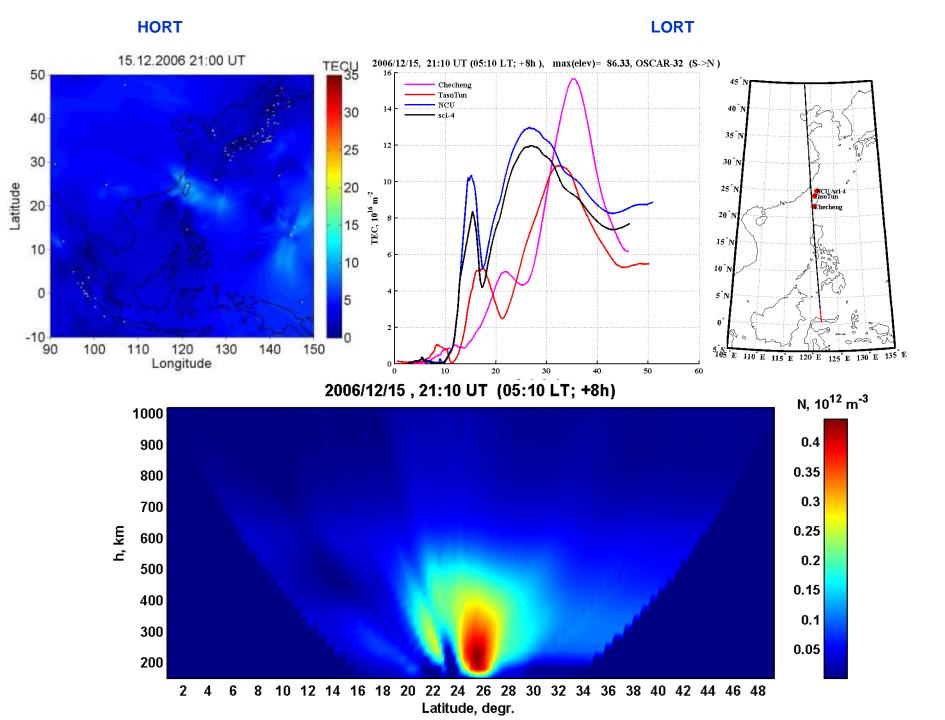


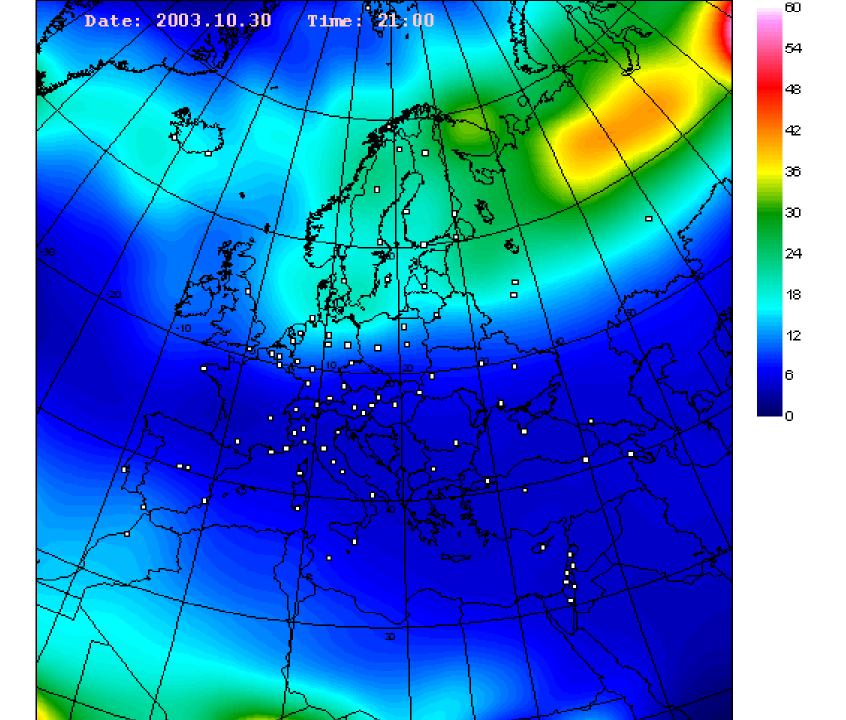
### **U.S. West Coast**

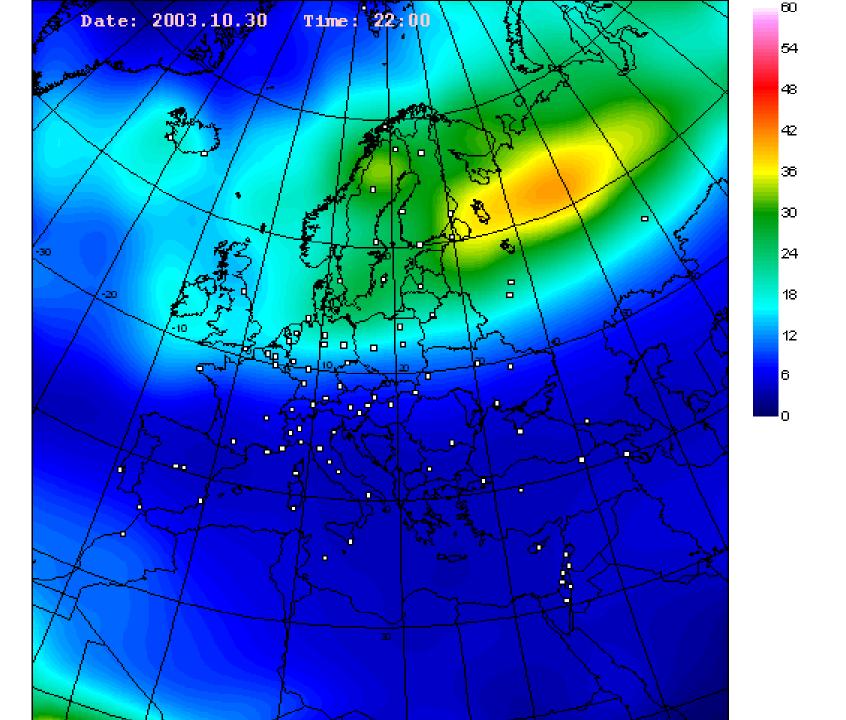


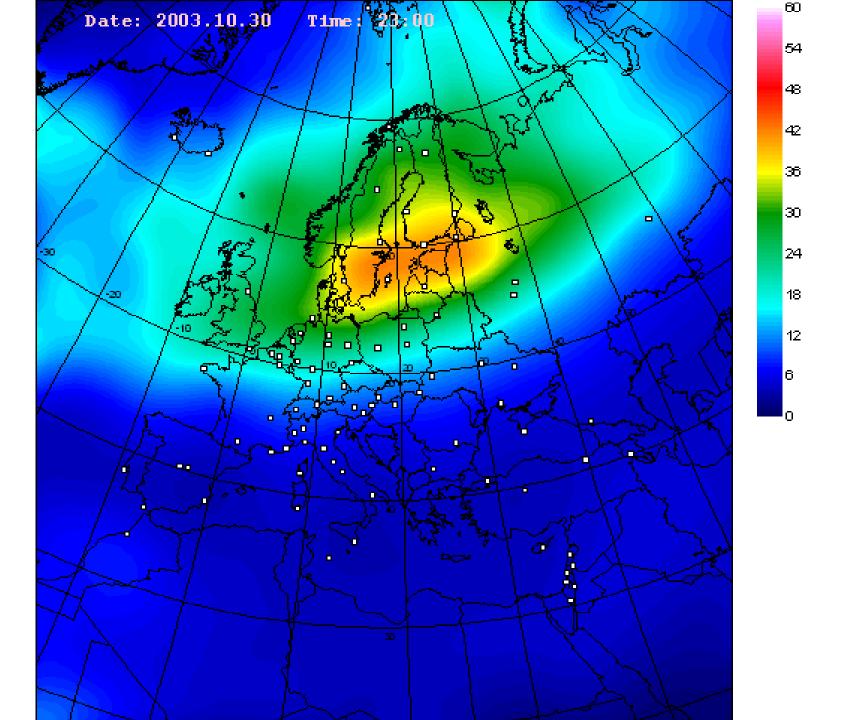
# Vertical TEC above South-East Asia according to 4D HORT during geomagnetic storm 15.12.2006 (18:00 UT-23:00 UT)

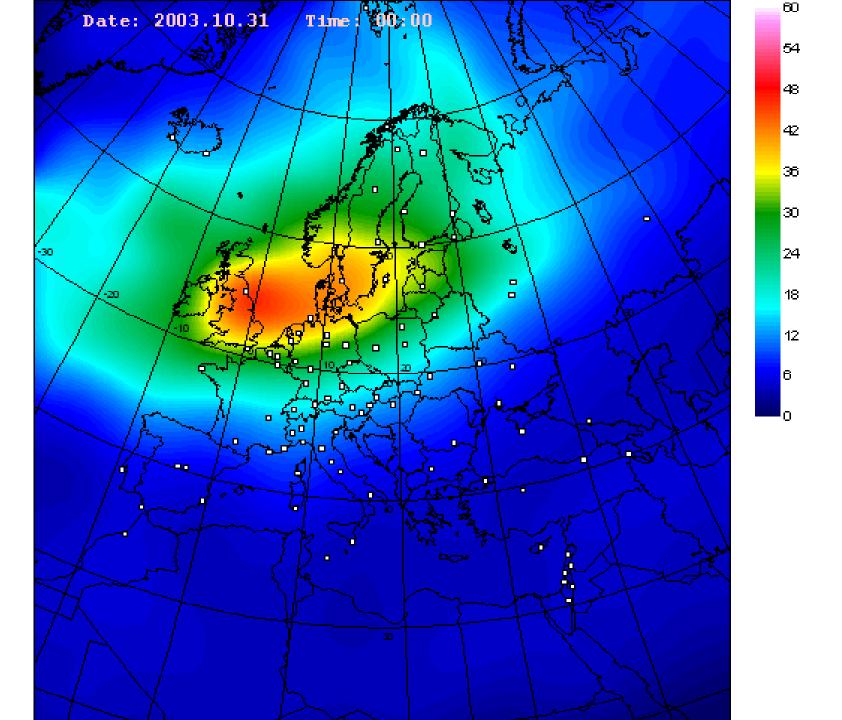


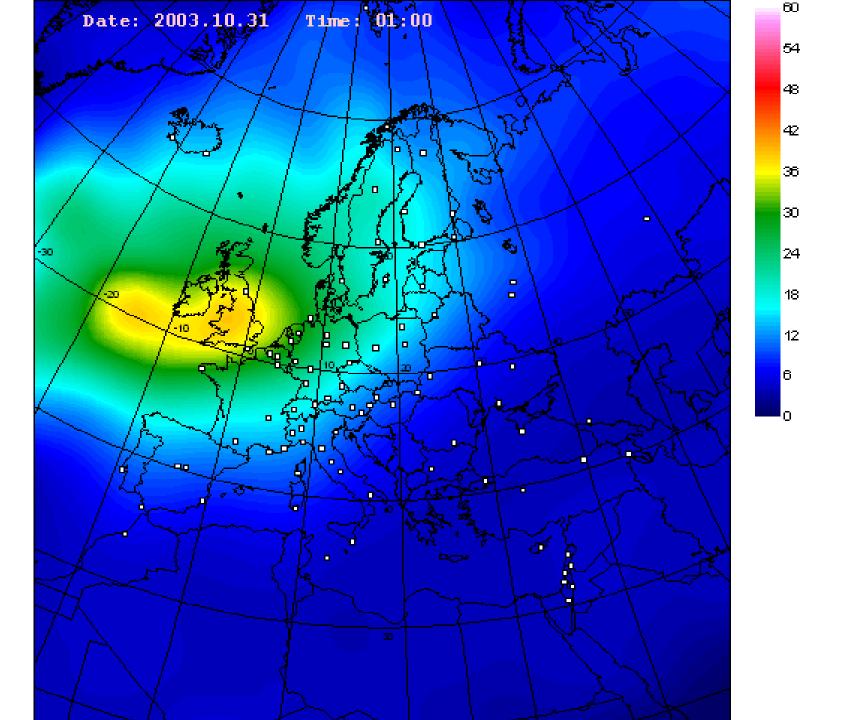




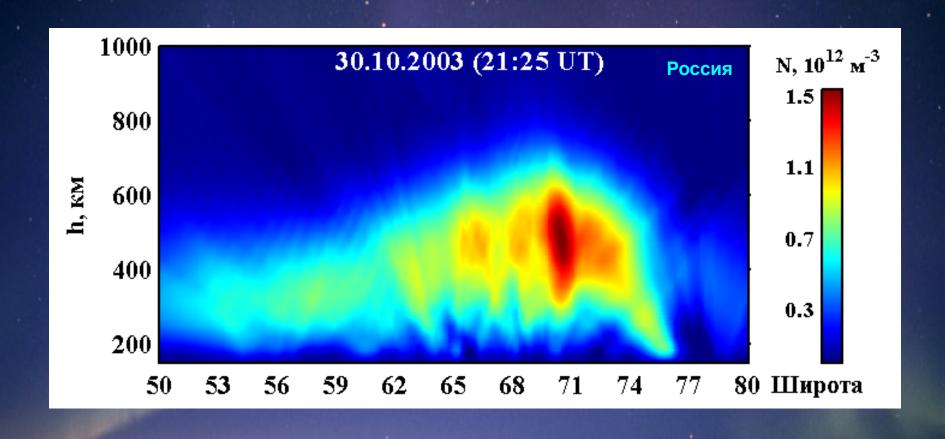




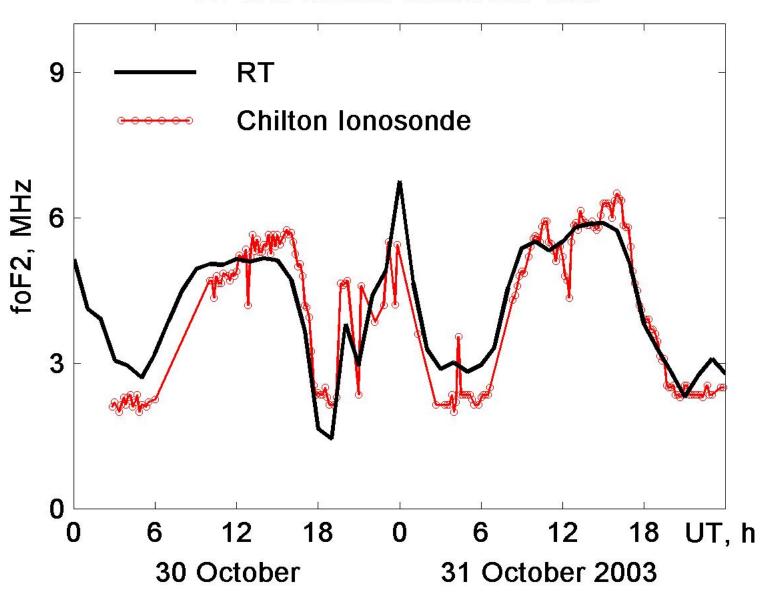




# **Solar Extreme Events of 2003**

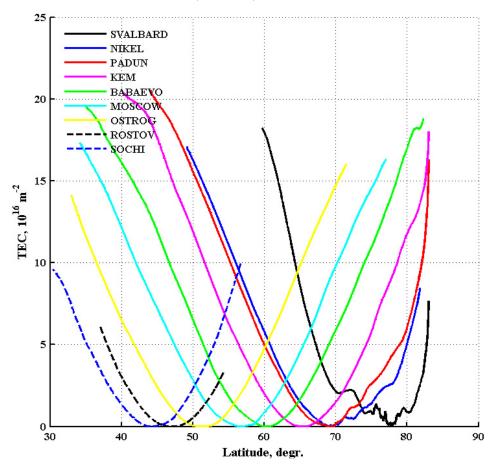


foF2 as obtained from RT and Chilton Ionosonde data



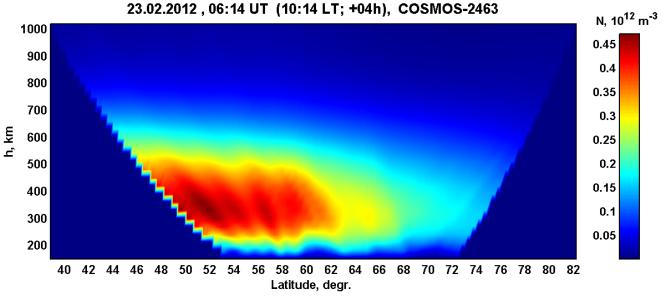
## Russian LORT system (Svalbard – Moscow - Sochi)



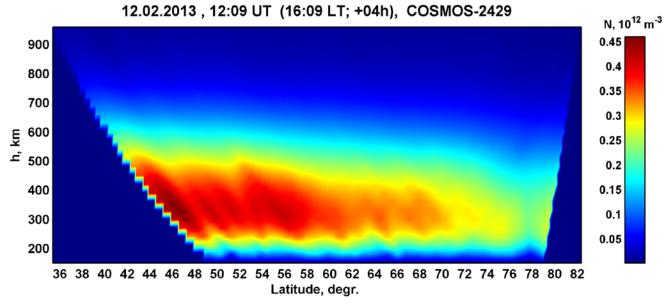




## **TIDs (Nortwest of Russia)**



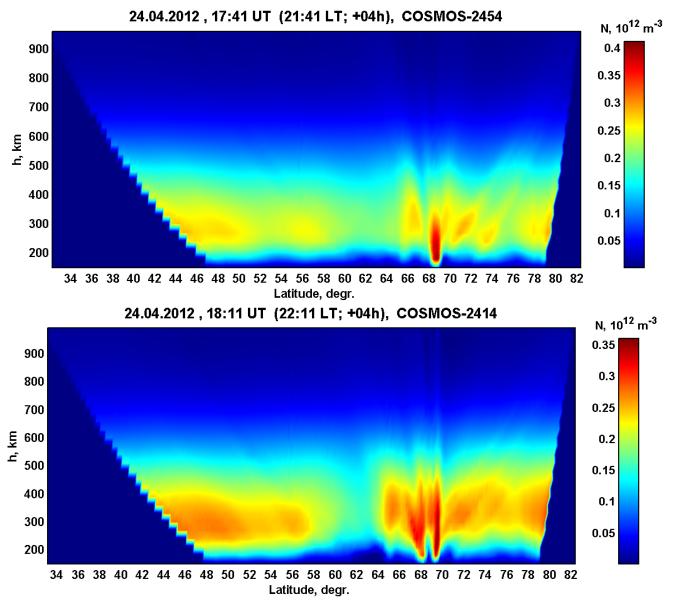
LORT image above Russian RT chain on February 23, 2012, 06:14 UT



LORT image above Russian RT chain on February 12, 2013, 12:09 UT

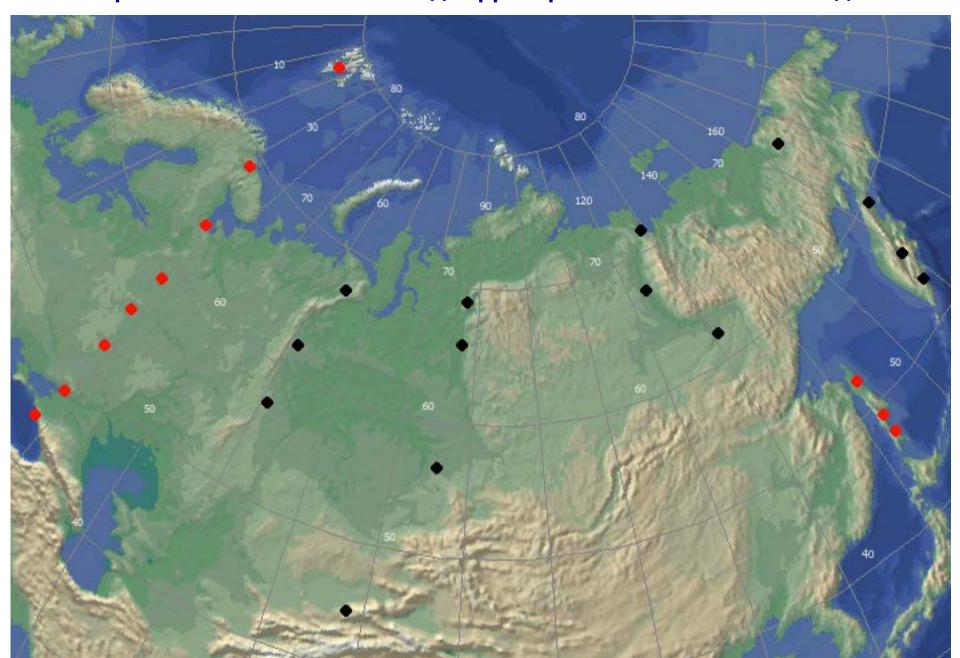
## **Region of Russian LORT system**

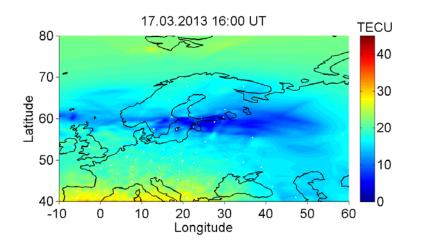
ionospheric features are probably associated with particle precipitation

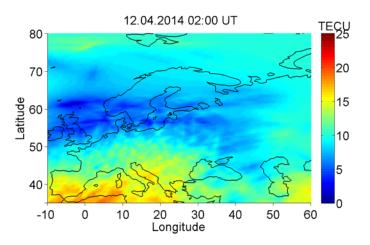


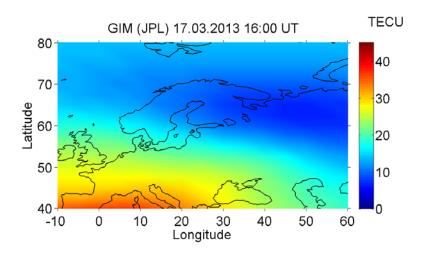
LORT images above Russian RT chain on April 24, 2012, 17:41 and 18:11 UT

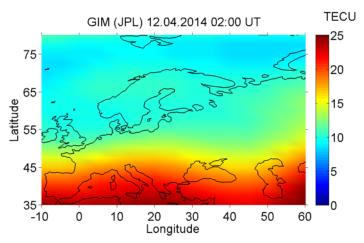
Система НОРТ. ФЦП "Создание системы мониторинга геофизической обстановки над территорией РФ на 2008-2015 годы"

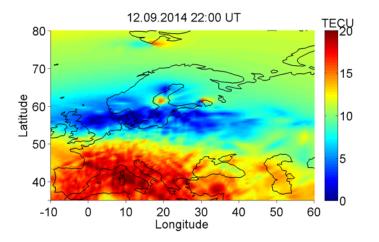


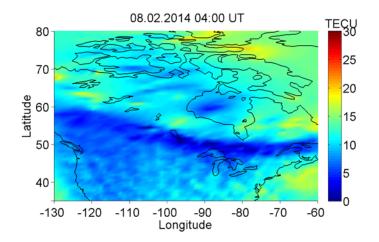


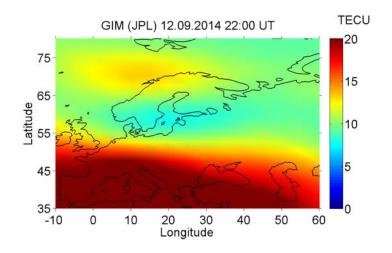


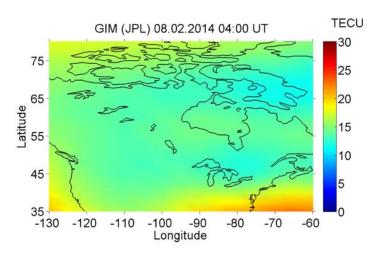


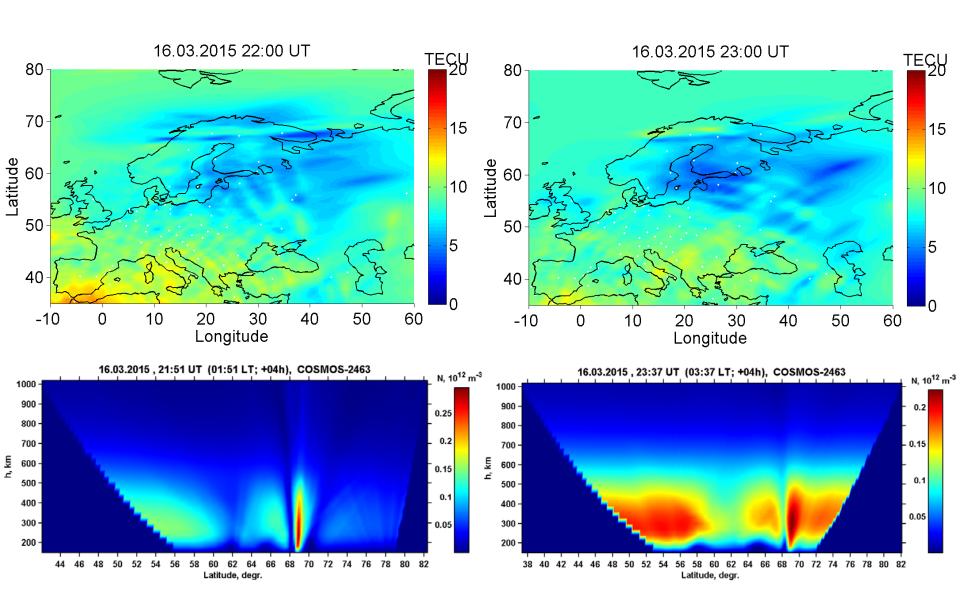


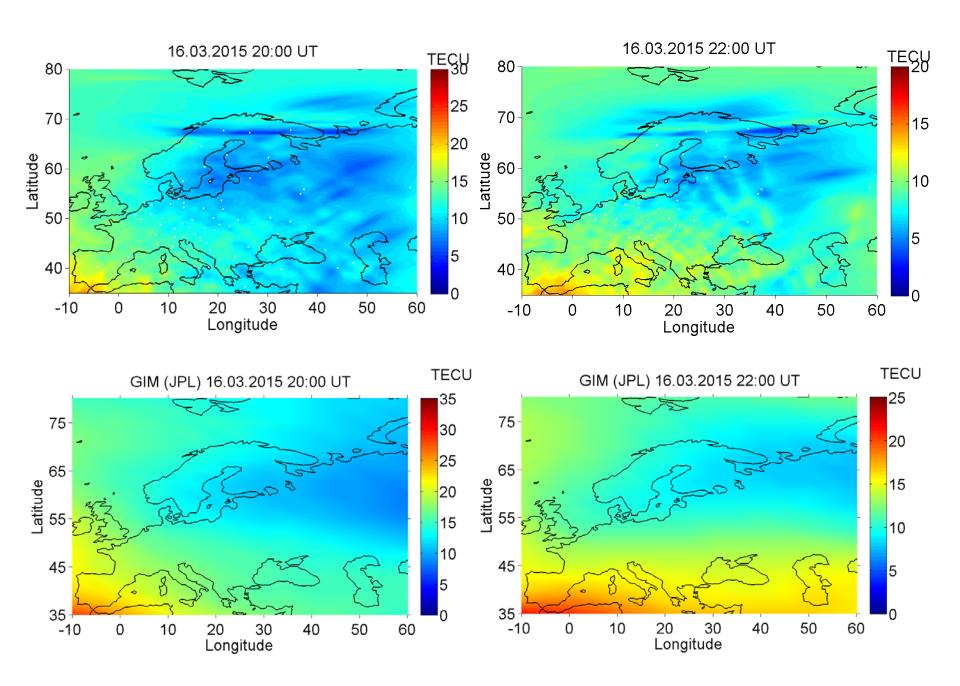


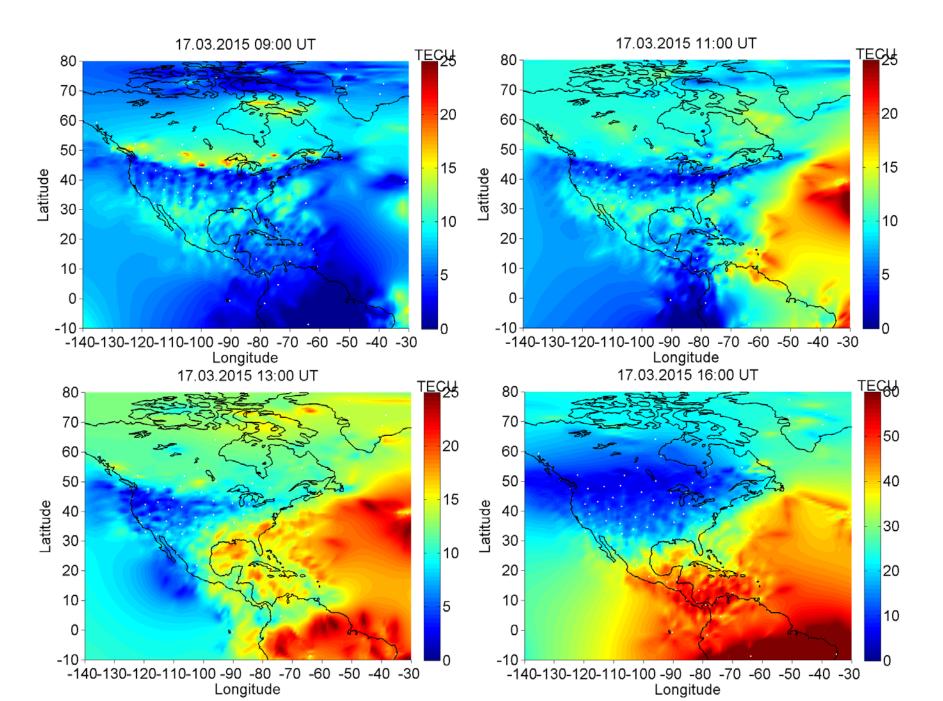


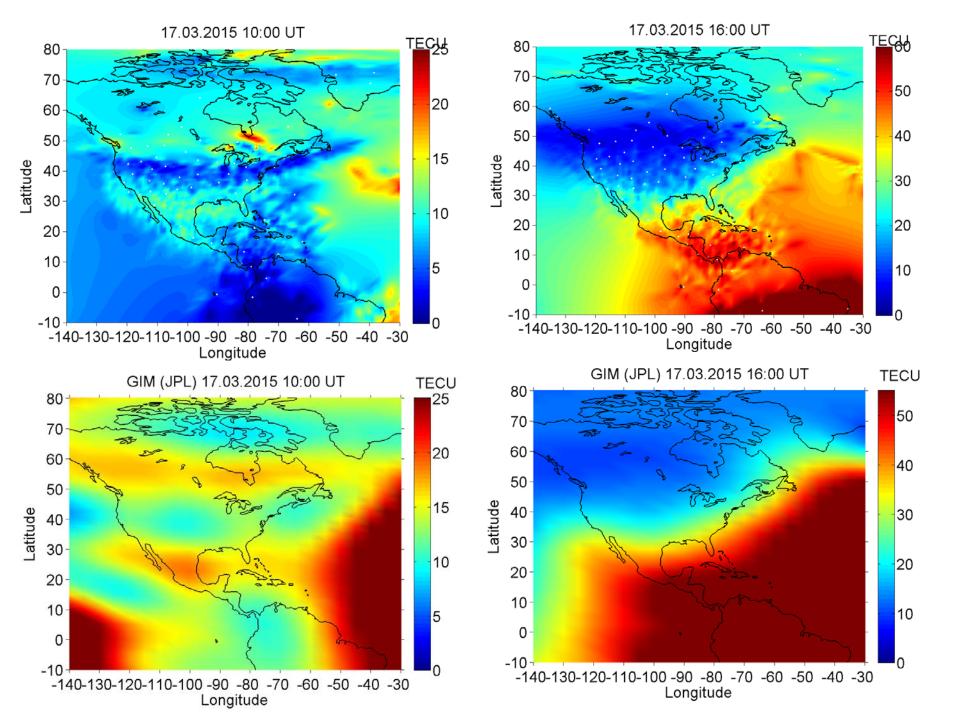




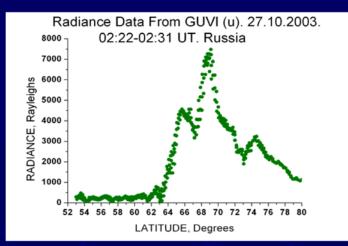


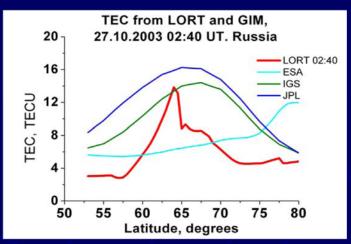






# Comparison of GUVI Data and TEC by LORT and GIM

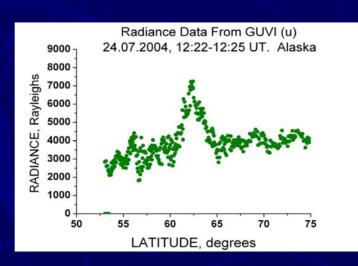


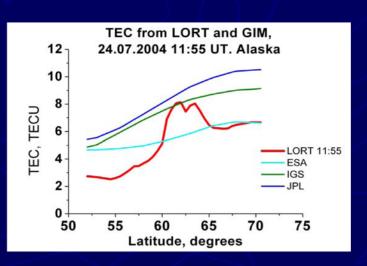


Dst=-47

Kp=3.3

**Ap=20** 

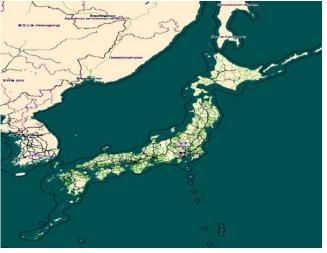




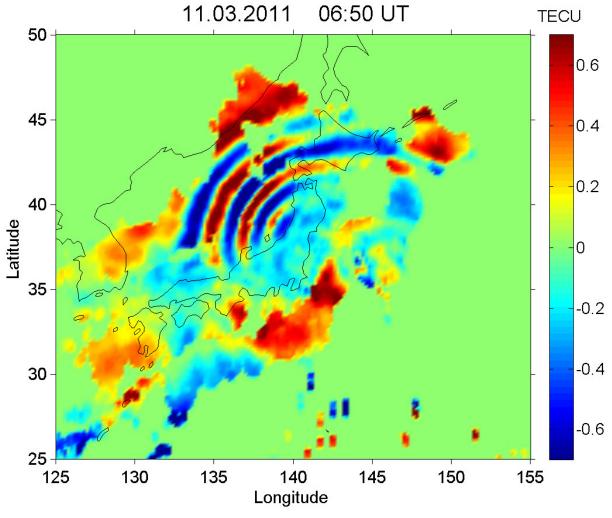
**Dst=-18** 

**Kp=6** 

Ap=80



# Tohoku mega-earthquake



The TEC waves, caused by the AGW from the Tohoku mega-earthquake, diverging from the epicenter of the event.

#### **SUMMARY**

- The combination of LORT and HORT systems provides significant advantages: HORT yields 3D distributions of the ionospheric plasma over vast regions, and LORT provides significantly higher resolution.
- The existing systems implementing the radio occultation (RO) approach (FormoSat-3/COSMIC and other systems that record the signals from the GPS/GLONASS satellites at HO satellites) provide the quasi tangential projections of electron density *N*.

The combination of the RT and RO methods, which supports the RT data by the probing data on the satellite-to-satellite paths (RO data), can significantly improve vertical resolution of RT reconstructions.

- The existing UV sounder systems (GUVI, SSULI) provide the integrals of *N* squared. In this case, the data from UV sounders can be incorporated into the common tomographic iterative scheme; however, the data should be consistent in terms of accuracy.
- GIM TEC data are generally smoother than the results provided by RT. The GIM TEC data during the severe geomagnetic disturbances should be used with caution.

#### **ACKNOWLEDGEMENTS**

We are grateful to the NWRA for providing the data from Alaska RT System and Taiwan National Central University for providing the data from Taiwan RT System and Radio-Hydro-Physics LLC for providing the data from West Coast US RT System. The GIM data were obtained through ftp://ftp.unibe.ch/aiub/ CODE/.