## Welfare and Trade Policy Exercise

James E. Anderson

Sept. 2006

A small open economy taxes its imports. Imports enter consumption but have no domestic counterpart. GDP consists of exports and a nontraded good, with Ricardian production, implying that the relative price of the nontraded good is invariant to tariffs in general equilibrium.

1. Show the invariance.

Good 0 (the nontraded good and and domestic consumption of exports, and any untaxed imports) is untaxed, while goods 1 and 2 are subject to tariffs. Preferences for consumption goods are described by a CES expenditure function  $e(\pi, u) = \Pi u$ ;  $\Pi = \left[ (\beta_0 \pi_0^*)^{1-\sigma} + (\beta_1 \pi_1)^{1-\sigma} + (\beta_2 \pi_2)^{1-\sigma} \right]^{1/(1-\sigma)}$ .

- 1. Show that  $e_i = \beta_i^{1-\sigma} (\pi_i/\Pi)^{-\sigma} u$  and that  $\pi_i e_{ij} \pi_j = -\sigma e(\delta_{ij} s_j) s_i$  where  $s_i = \pi_i e_i/e = \beta_i^{1-\sigma} (\pi_i/\Pi)^{1-\sigma}$ , the expenditure share on good *i*.
- 2. Derive a useful expression for  $B_2$ .
- 3. Derive an expression for the shadow price of foreign exchange.
- 4. Show that the concertina rule holds for this economy.
- 5. Suppose that all external prices are equal to one, and  $\beta_0 = 0.75$ ,  $\beta_1 = 0.15$ ,  $\beta_2 = 0.10$ . g = 100 and the external transfer is equal to zero. Tariff revenue is redistributed to the representative consumer. Initially,  $\pi_1 = 1.5$ ,  $\pi_2 = 1.1$ . The elasticity of substitution  $\sigma$  is equal to 2. Solve for the initial level of welfare. (This requires a calculator or computer program.) Solve for  $B_1$  and  $B_2$ .

- 6. Solve for the welfare equivalent uniform tariff and the trade-weighted average tariff. (The former calculation requires a computer or programmable calculator capable of implicit solutions.)
- 7. Plot the welfare contours in tariff factor space for this economy, and the locus of 'best' tariffs for each good given a fixed tariff for the other good. (In principle you could generate these with an appropriate programming in GAUSS or Mathematica, but a qualitative sketch is sufficient.)
- 8. Suppose that a fixed amount of revenue must be raised with tariffs. Show that the (Ramsey) optimal tariff structure is uniform.