

# Statistical Characterization of GNSS Signal Carrier Doppler Frequency Deviations During Ionospheric Scintillation

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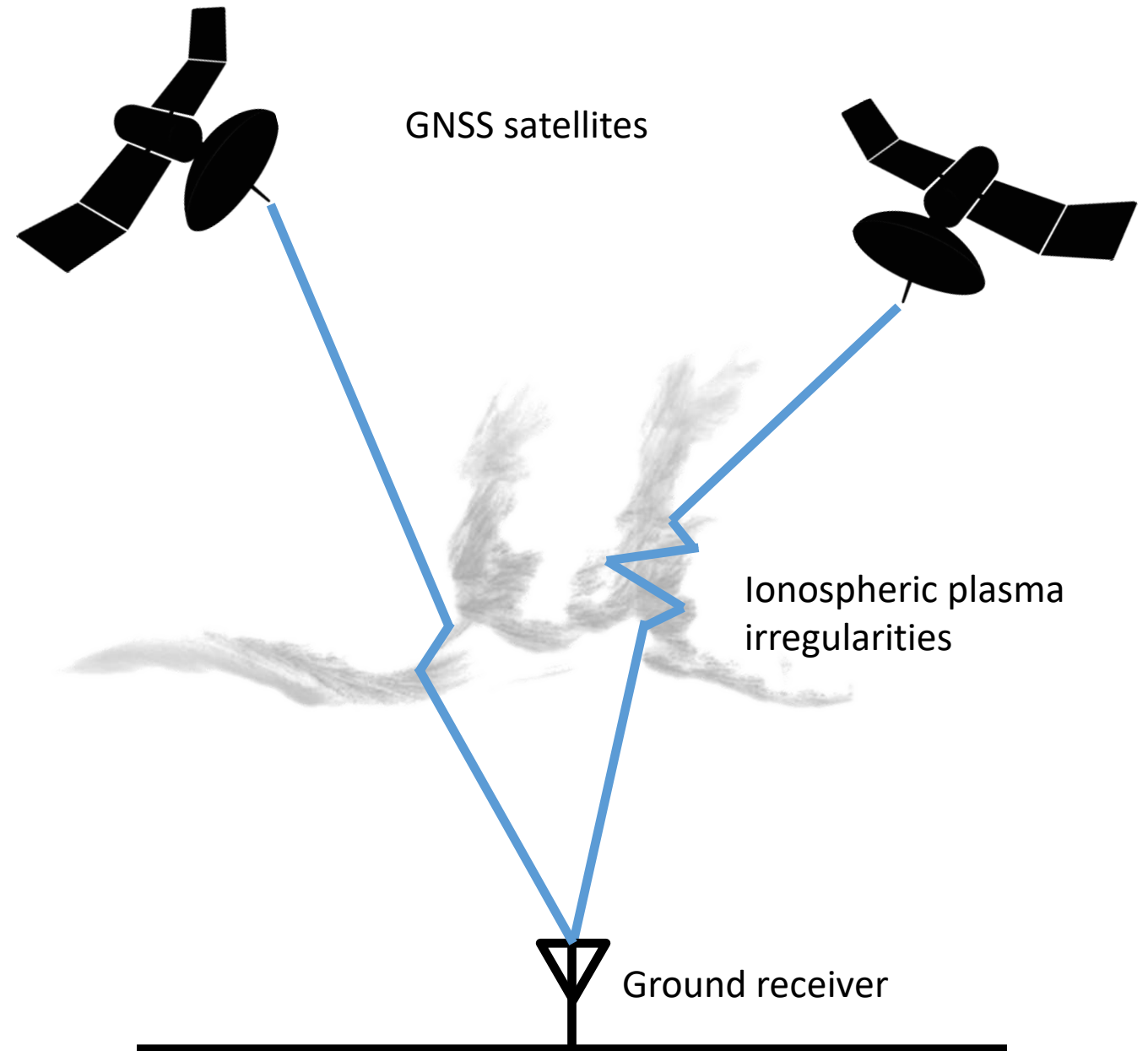


# Outline

- Overview of ionospheric scintillation
- Motivation: GPS receiver carrier tracking
- Experiment setup
- Description of data processing procedure
- Low and high latitude results
- Future work

# Ionospheric Scintillation

Small-scale irregularities in the density of electrons cause fluctuations in the **amplitude, phase, and frequency** of a GNSS signal.



# Ionospheric Scintillation Indices

Ionospheric scintillation indices are statistical measures of the severity of scintillation.

$S_4$ , defined as the normalized standard deviation of the detrended signal intensity, quantifies the effect of scintillation on signal amplitude:

$$S_4 = \sqrt{\frac{\langle SI^2 \rangle - \langle SI \rangle^2}{\langle SI \rangle^2}}$$

$\sigma_\phi$ , defined as the standard deviation of the detrended carrier phase, quantifies the effect on signal phase:

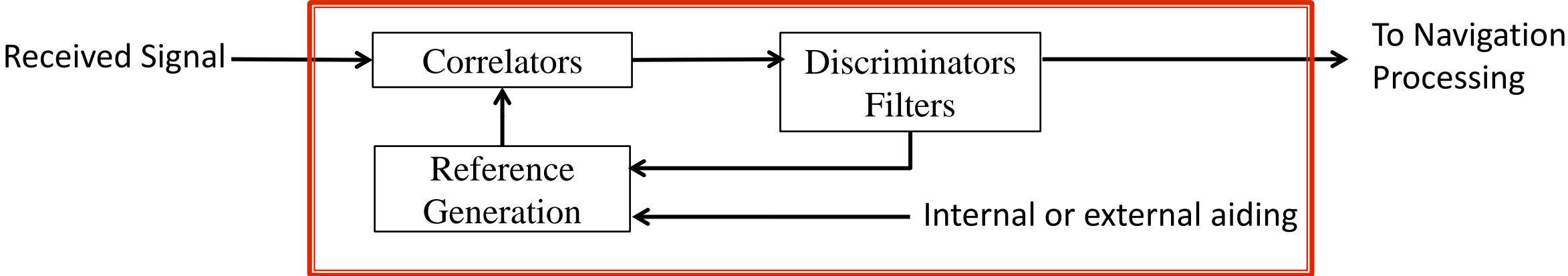
$$\sigma_\phi = \sqrt{\langle \phi^2 \rangle - \langle \phi \rangle^2}$$

**Low latitudes** experience deep amplitude fading ( $S_4$ ) and large phase fluctuations ( $\sigma_\phi$ ).

At **high latitudes**, scintillation effects are dominated by phase fluctuations ( $\sigma_\phi$ ).

The effect of scintillation on **carrier Doppler frequency** is less studied.

# Receiver Carrier Tracking



Processing Component	Correlator	Estimator	Filter
Example Design Parameters	Integration Time	Estimator Type	Bandwidth
Deep Fade → Weak Signal	Long	Phase	Narrow
Fast Carrier Phase Change → Highly Dynamic Signal	Short	Frequency	Wide

# Experiment Setup

## GPS L1 (1575.42 MHz) Data



**Ascension Island**  
7.93°S, 14.37°W

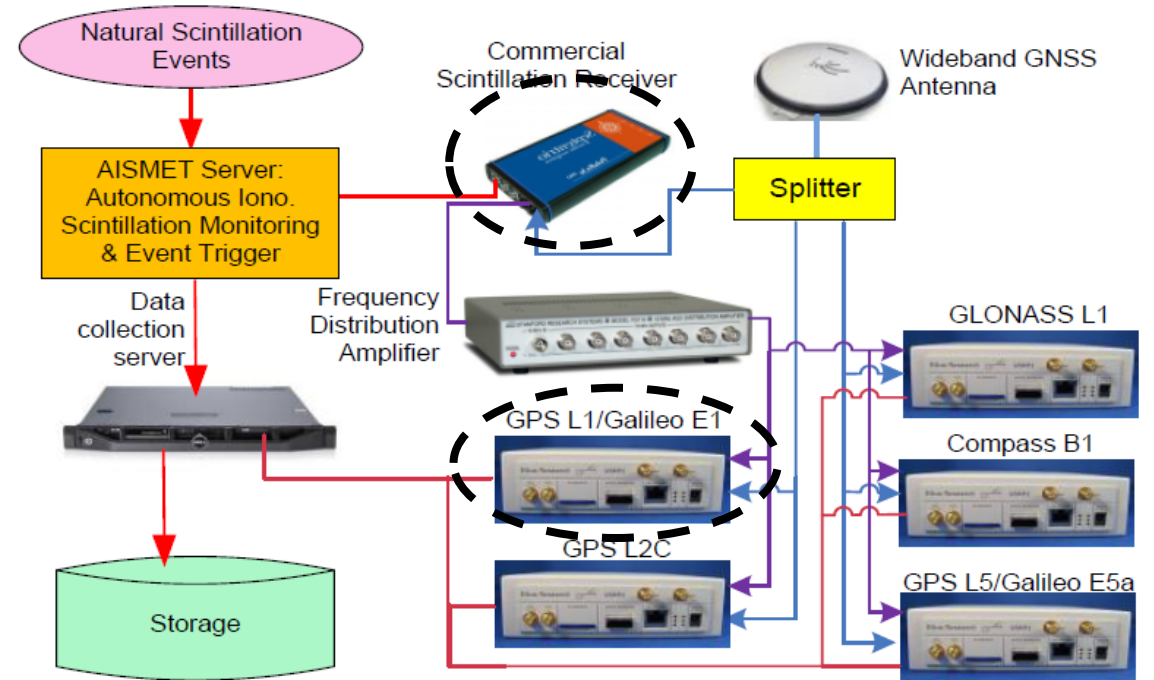


Figure: Mark Carroll

About 5 hours of total data:

- PRN 24 on 03/08/13
- PRN 29 on 03/09/13
- PRNs 24 and 31 on 03/10/13

Collected with Septentrio PolaRxS receiver and custom hardware

# Experiment Setup

**Poker Flat Research Range, Alaska**  
65.14°N, 148.01°W



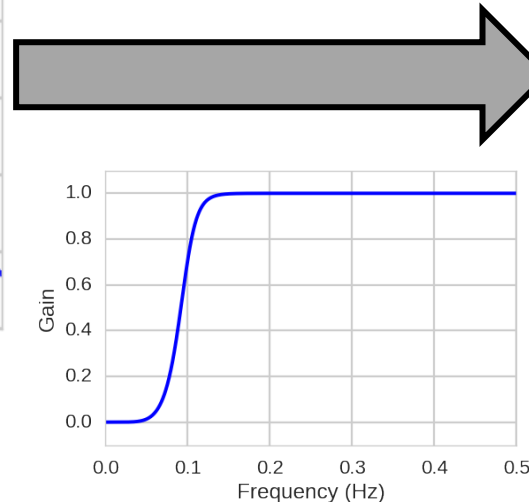
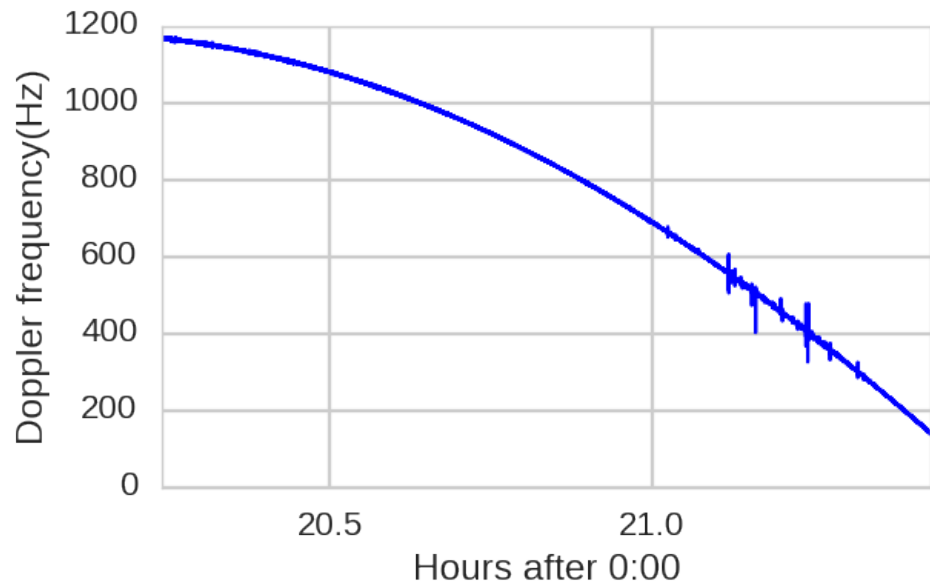
One full day (12/20/2015) of  
data collected by Septentrio  
PolaRxS receiver



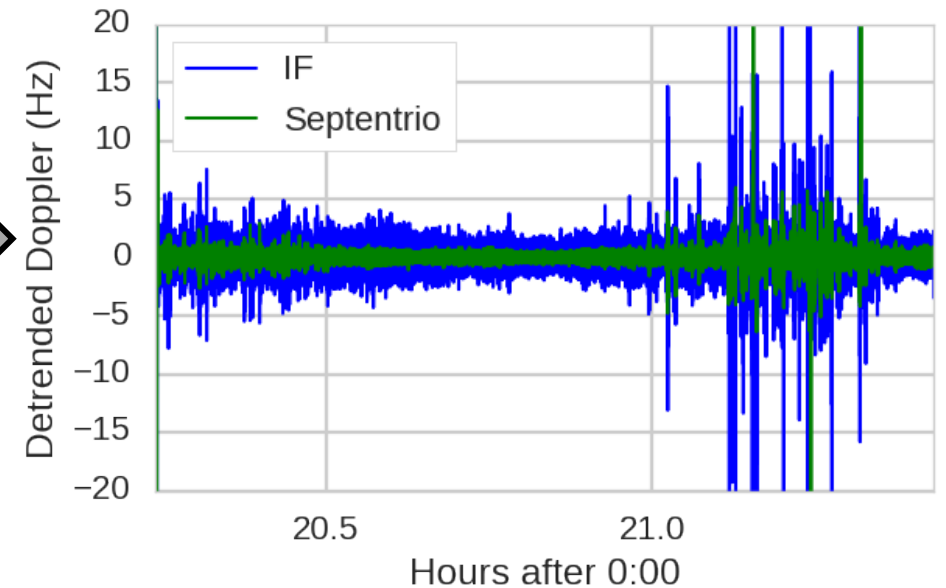
# Data Processing Procedure – Doppler Detrending

**Example low-latitude data** (PRN 24 passing over Ascension Island on 03/10)

**1** Differentiate the carrier phase to find Doppler frequency



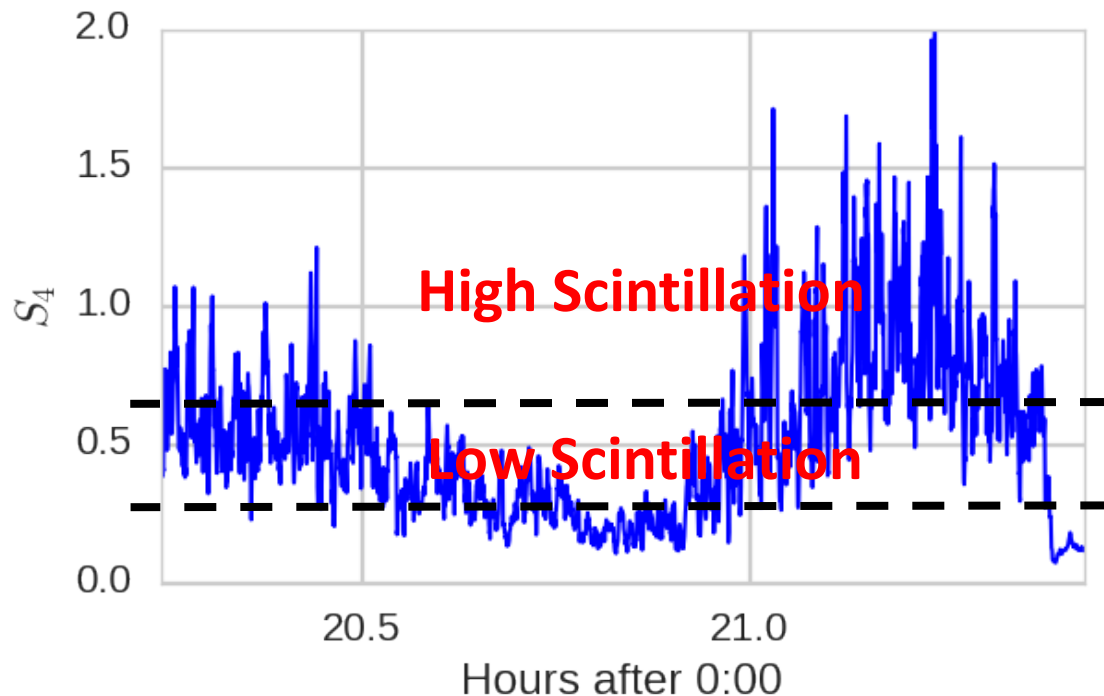
**2** Detrend using a sixth-order Butterworth Filter





# Data Processing Procedure – Scintillation Index

- ③ Calculate the appropriate scintillation index



Low latitude data:  $S_4$   
High latitude data:  $\sigma_\phi$

- ④ Categorize Doppler deviations per corresponding level of scintillation

**Low scintillation regime:**

$$0.3 \leq S_4 < 0.6 \text{ or } 0.2 \text{ rad} \leq \sigma_\phi < 0.5 \text{ rad}$$

**High scintillation regime:**

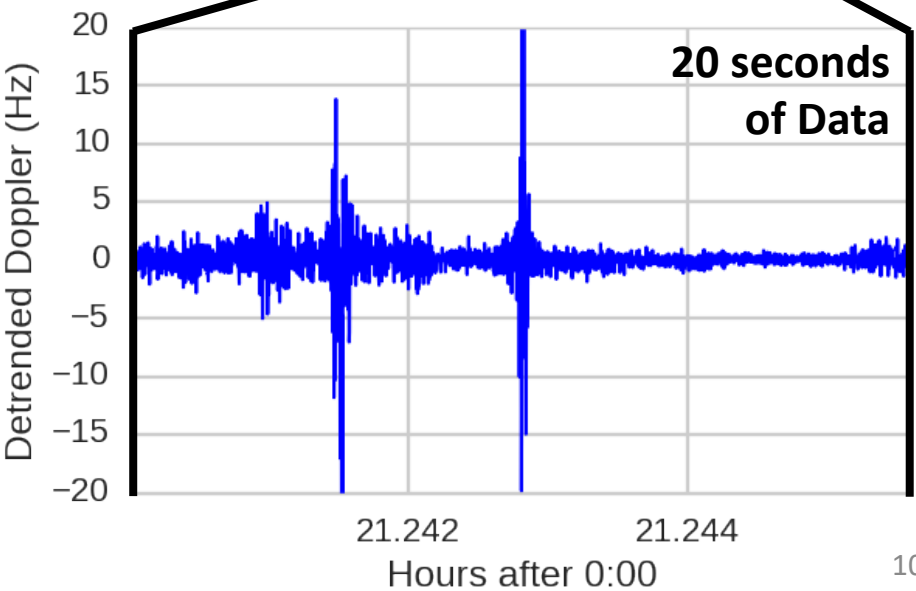
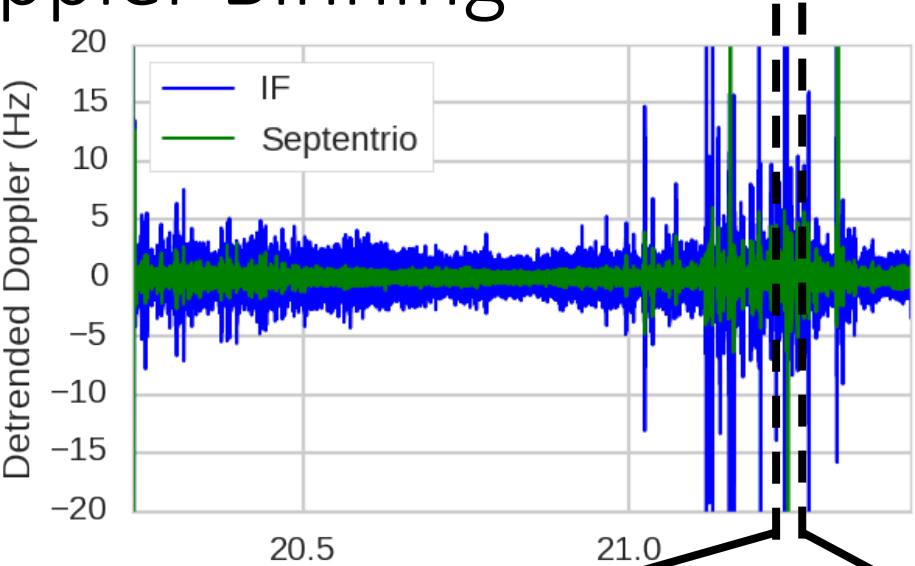
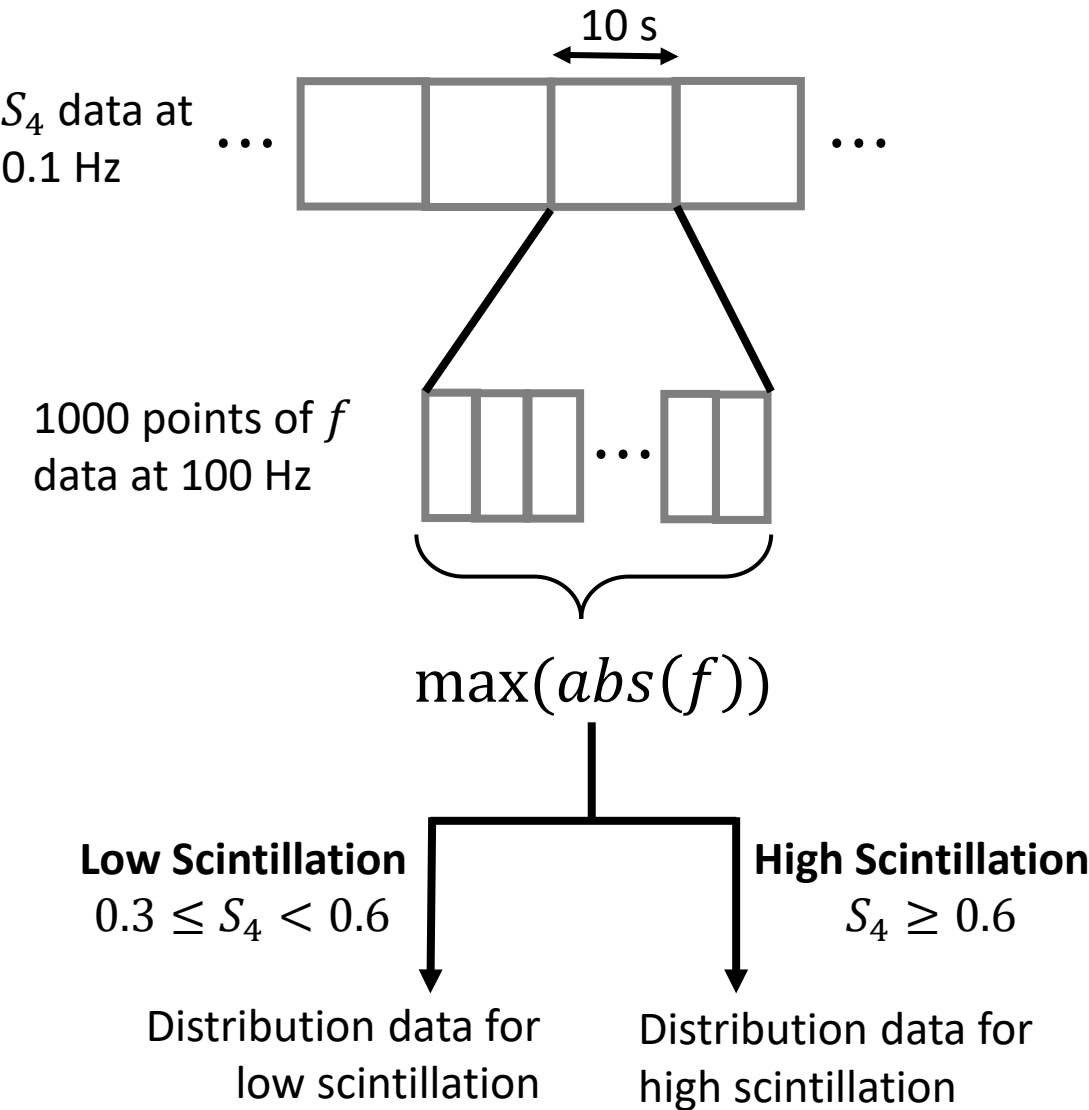
$$S_4 \geq 0.6 \text{ or } \sigma_\phi \geq 0.5 \text{ rad}$$

The rate of  $S_4$  and  $\sigma_\phi$  is 0.1 Hz

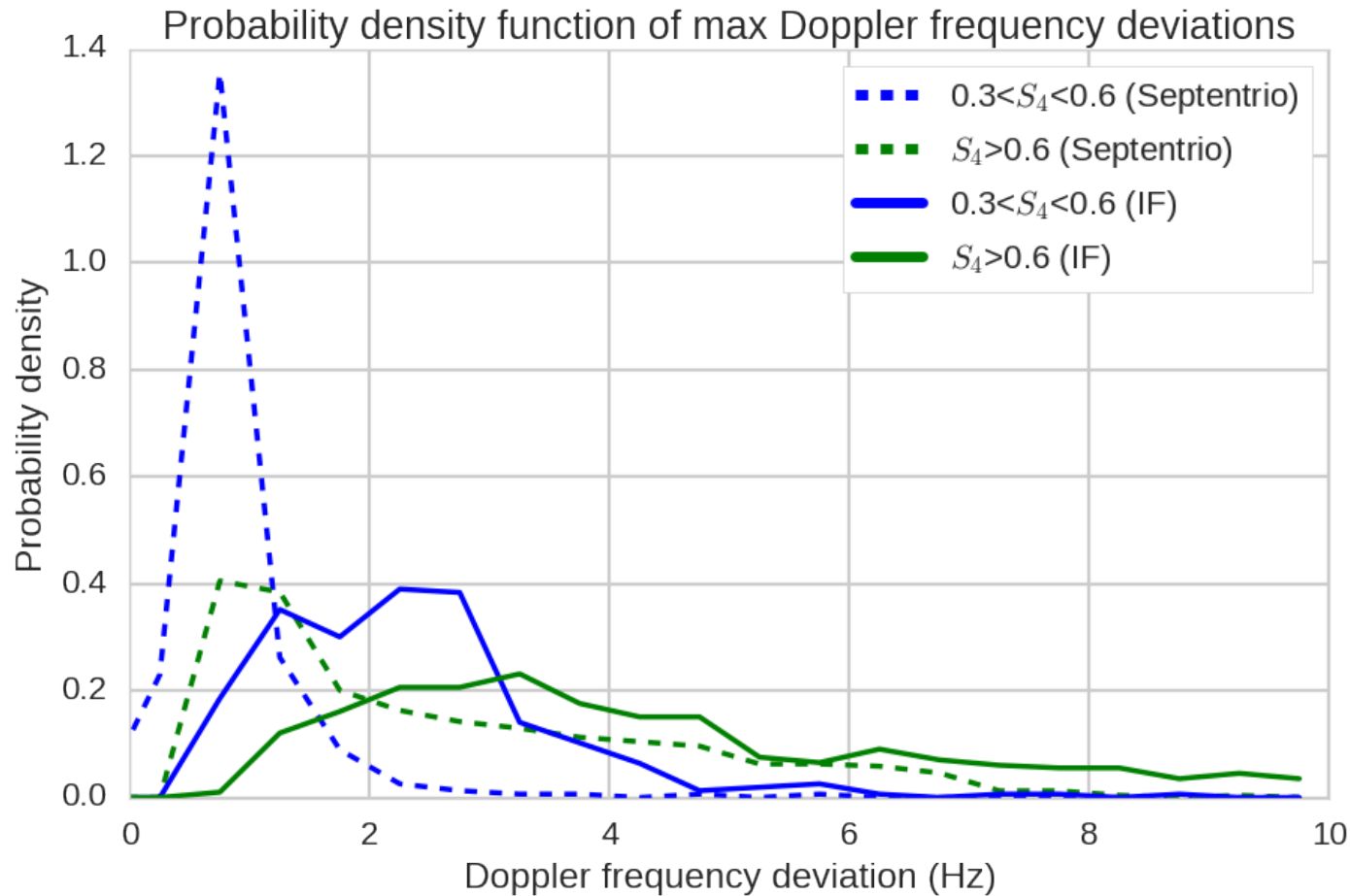
The rate of detrended Doppler is 100 Hz

**1000 points of Doppler for each point of the scintillation index**

# Data Processing Procedure – Doppler Binning



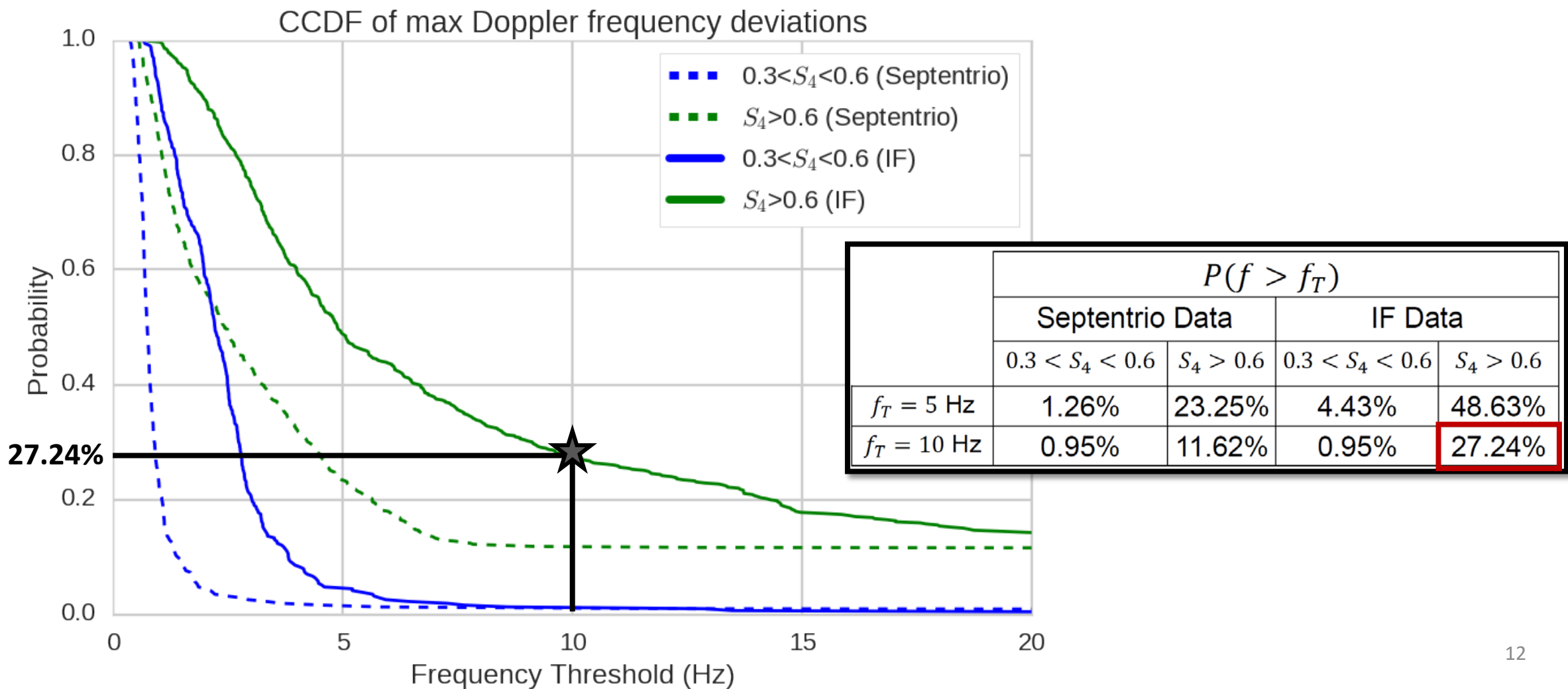
# Low Latitude Results



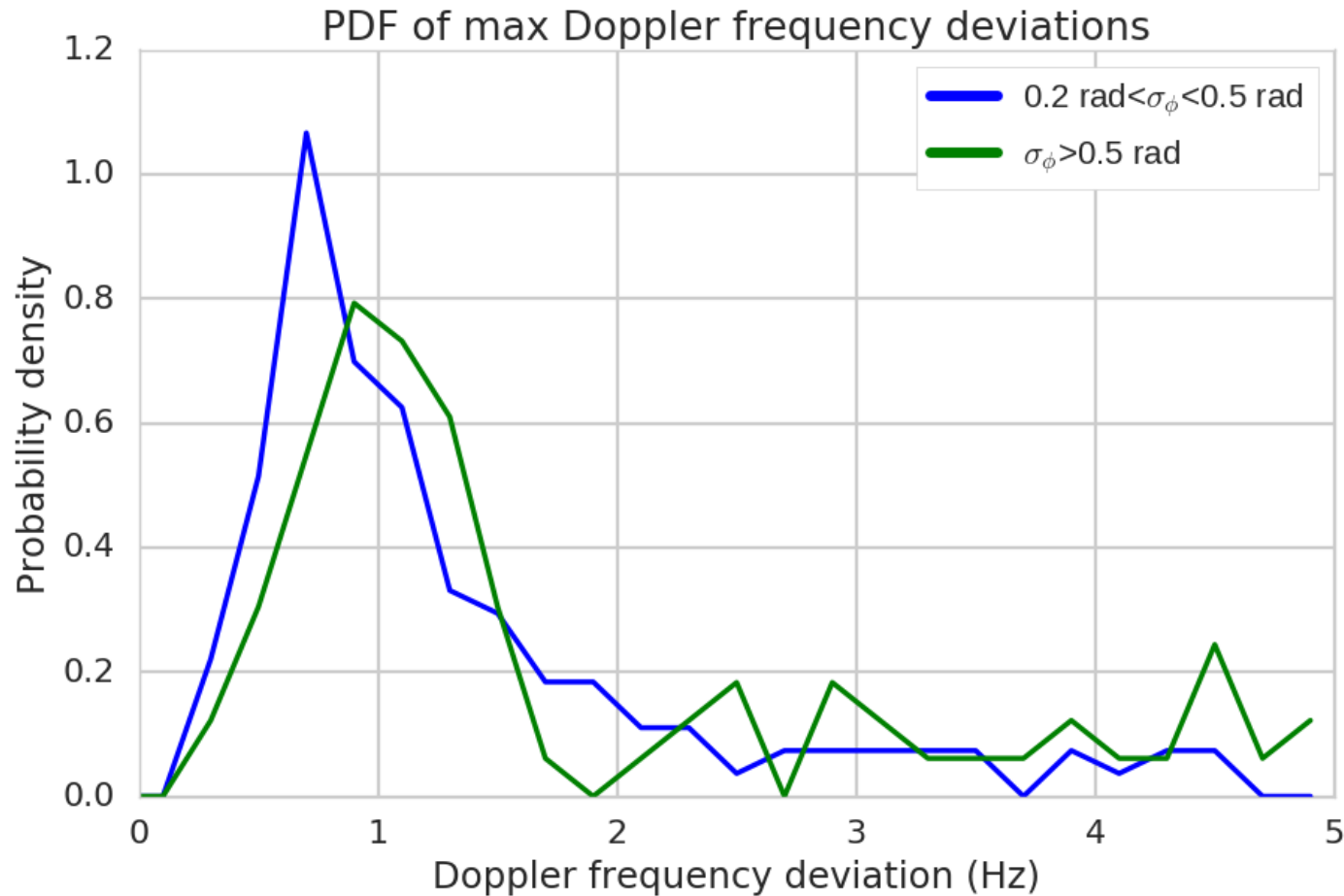
- Higher magnitude Doppler frequency deviations are **more probable** in the **high scintillation regime** than in the low scintillation regime
- Septentrio measurements underestimate the magnitude of the deviations

# Low Latitude Results

Complementary continuous distribution function: **What is the probability that the detrended Doppler frequency will experience a deviation greater than some threshold value?**



# High Latitude Results



Higher magnitude Doppler frequency deviations are **more probable** in the **high scintillation regime** than in the low scintillation regime.

# Future Work

- Process signals from GPS L2 and L5 bands
- Process signals from other GNSS constellations (Galileo, GLONASS, BeiDou)
- Use data from a wider range of days throughout the year
  - Explore seasonal variation
- Collect data from a variety of different locations

Questions? Comments?

# Bibliography

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# Graphics Credit

- Satellite: <http://www.clker.com/cliparts/f/b/n/e/r/3/satellite-hi.png>
- Globe: [https://img.clipartfest.com/10869fa307ba19d6d13aef9e906b5c0a\\_transparent-world-globe-globe-world-clipart\\_4021-4021.png](https://img.clipartfest.com/10869fa307ba19d6d13aef9e906b5c0a_transparent-world-globe-globe-world-clipart_4021-4021.png)
- Pin: <http://www.clipartbest.com/cliparts/niB/GXK/niBGXKRxT.png>
- Spread f: <http://landau.geo.cornell.edu/data/F040223.gif>
- Poker flat: [http://www.thelivingmoon.com/45jack\\_files/04images/Poker\\_Flat/2577899.jpg](http://www.thelivingmoon.com/45jack_files/04images/Poker_Flat/2577899.jpg)
- PolaRxS: <http://www.navtechgps.com/assets/item/large/PolaRxS-IMG60431.jpg>